

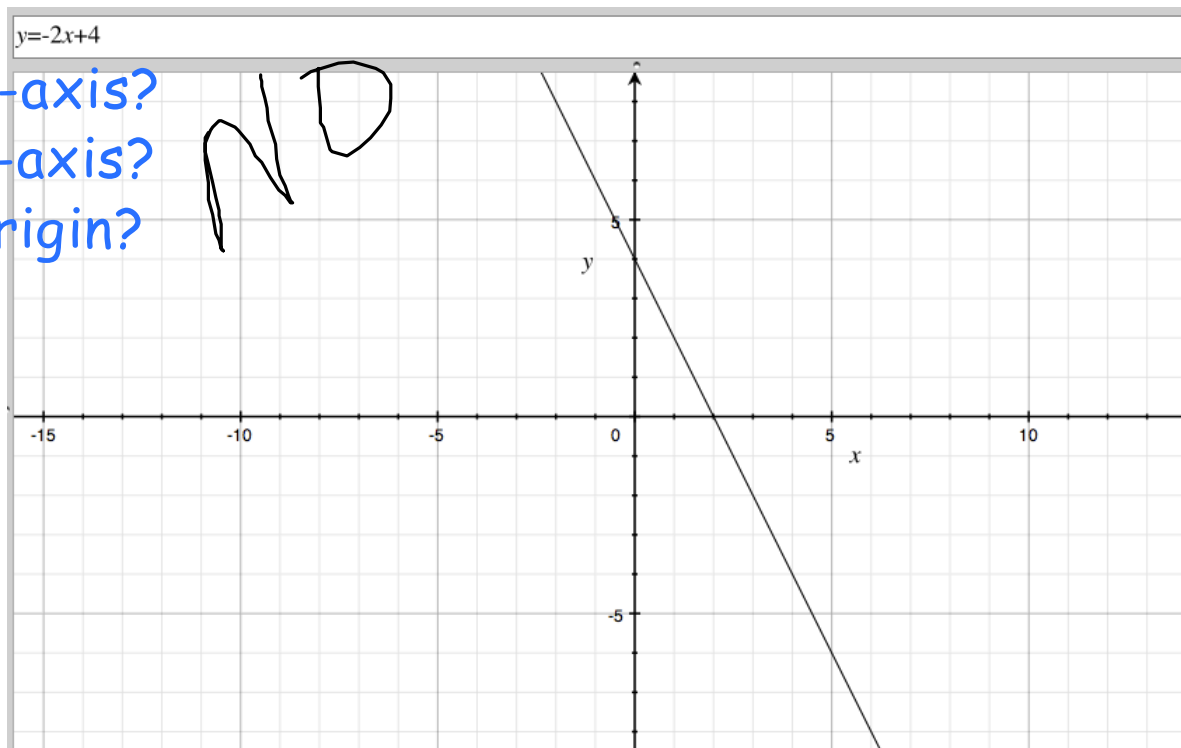
Unit 12
Day 8
Symmetry

A function whose graph is symmetric with respect to the Y-AXIS is called an EVEN FUNCTION.

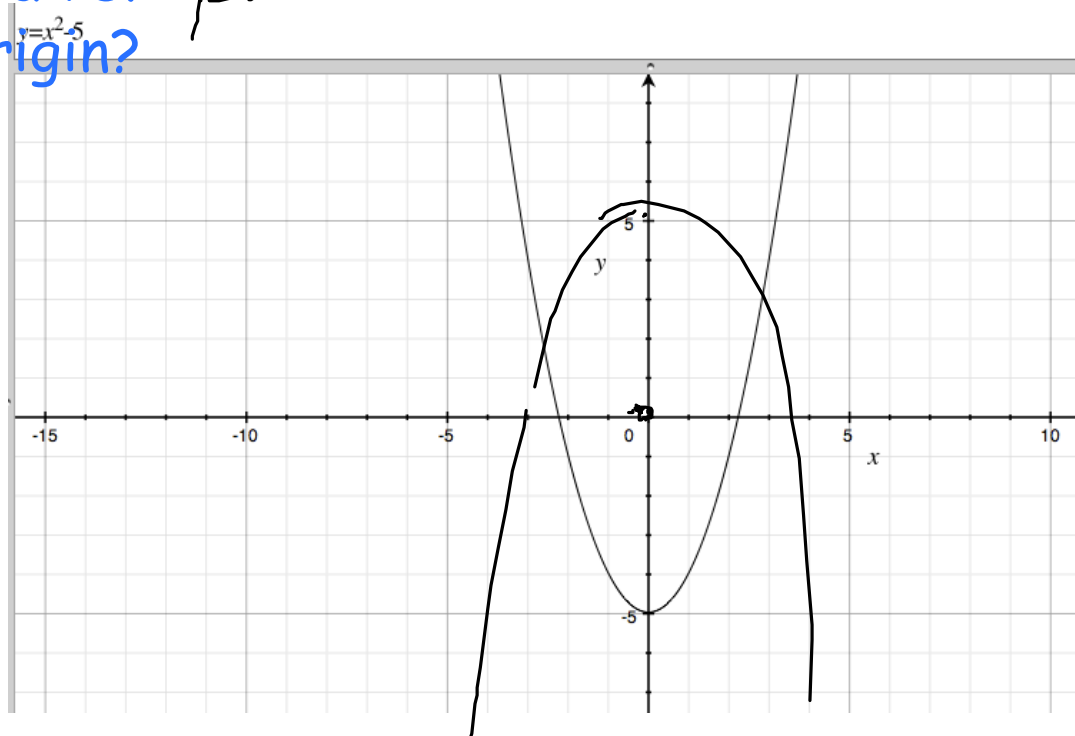
A function whose graph is symmetric with respect to the ORIGIN is called an ODD FUNCTION.

Symmetric to x-axis?
Symmetric to y-axis?
Symmetric to origin?

NO



Symmetric to x-axis? NO
Symmetric to y-axis? YES
Symmetric to origin? NO



Function?

NO

Symmetric to x-axis?

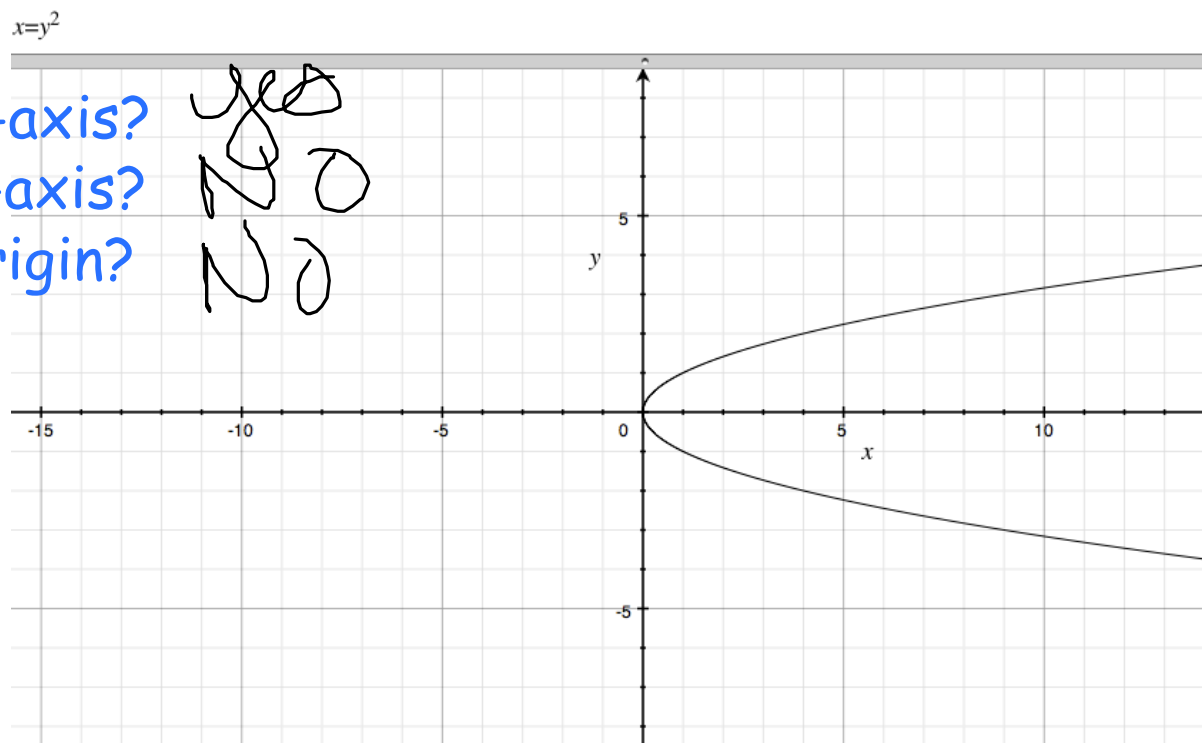
Yes

Symmetric to y-axis?

NO

Symmetric to origin?

NO



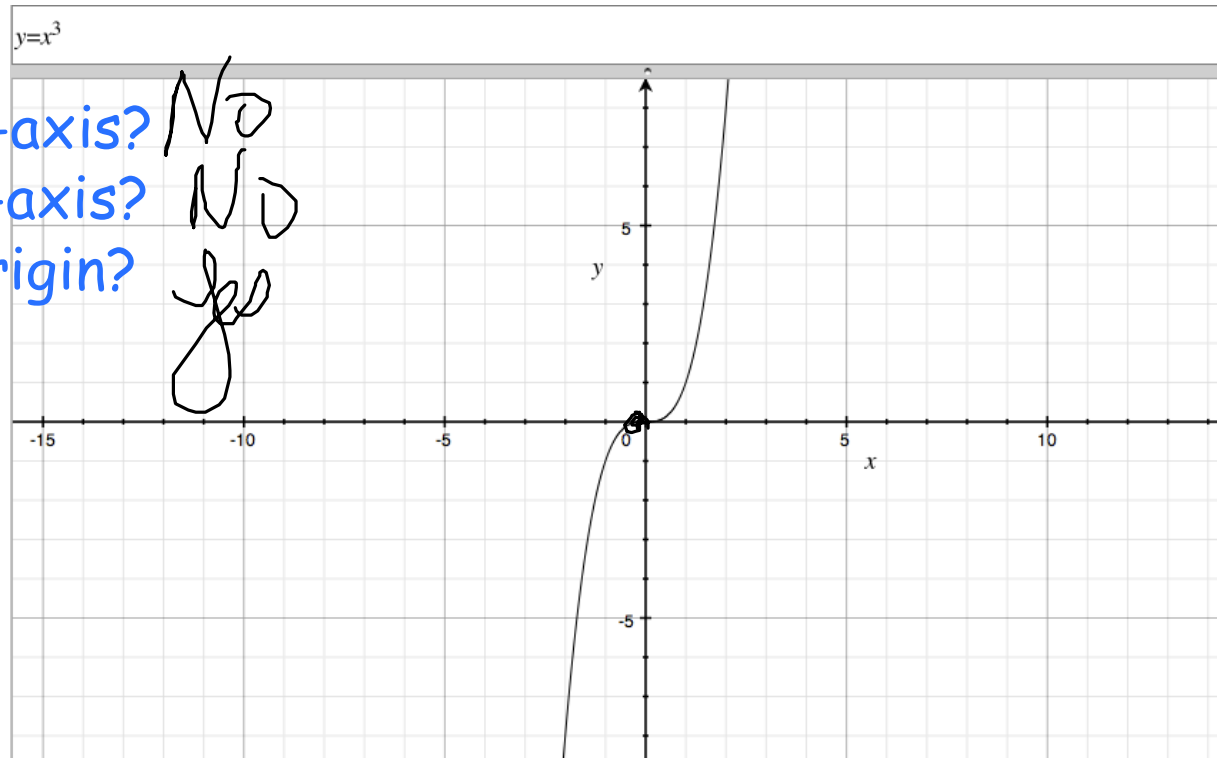
Function?

Yes

Symmetric to x-axis? No

Symmetric to y-axis? No

Symmetric to origin? Yes



Function?

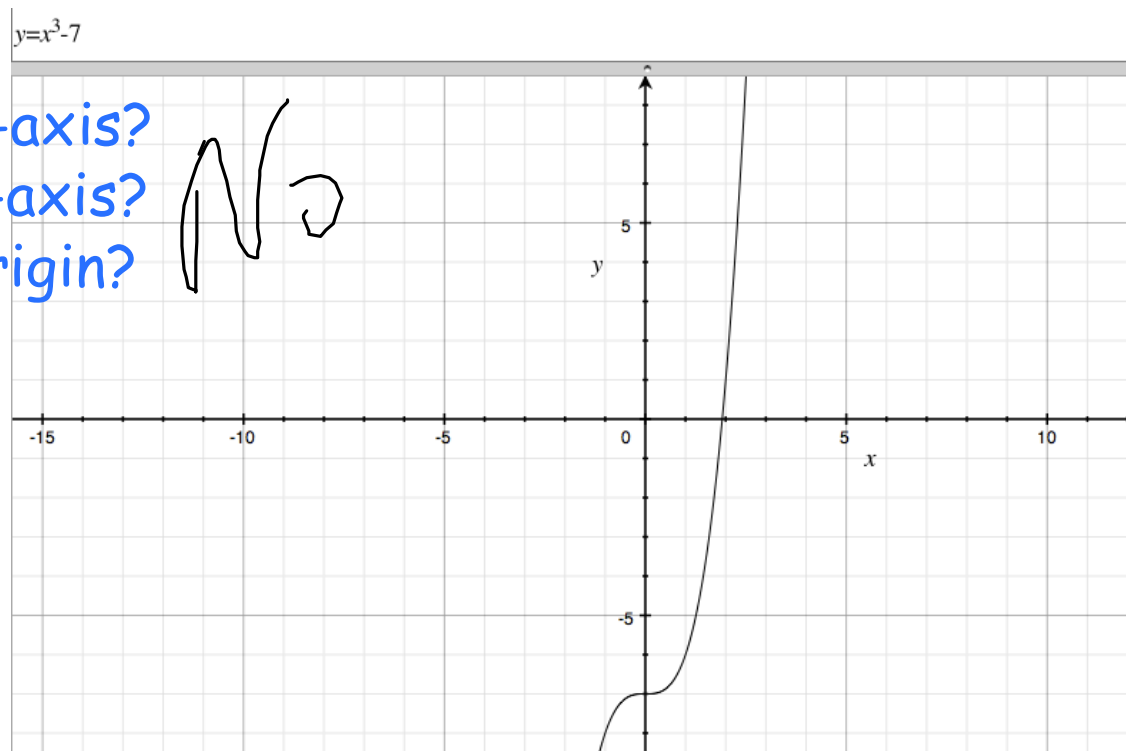
yes

Symmetric to x-axis?

Symmetric to y-axis?

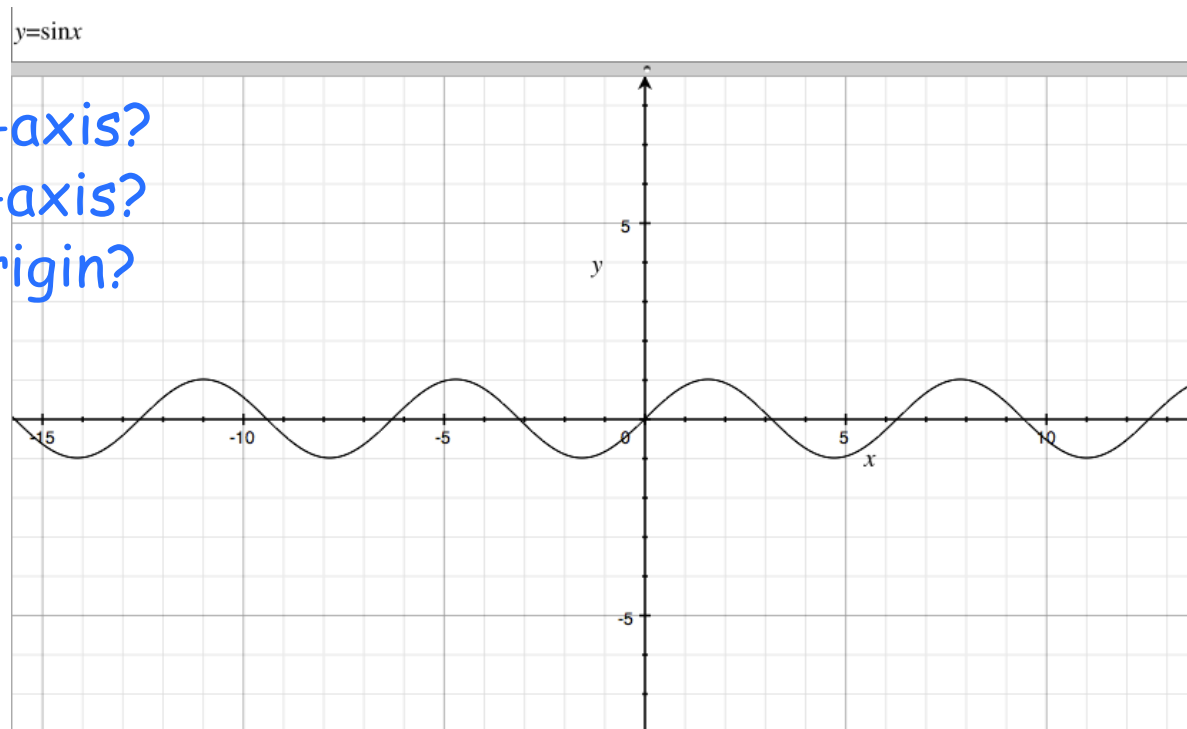
Symmetric to origin?

No



Function?

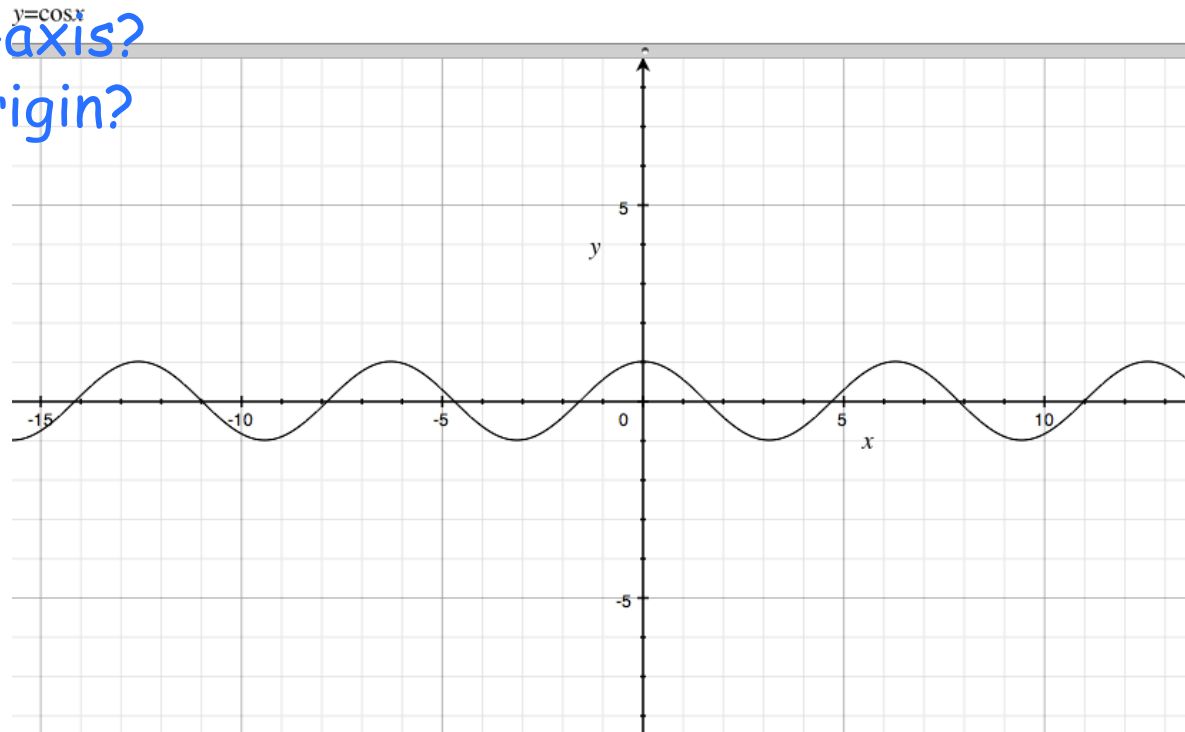
Symmetric to x-axis?
Symmetric to y-axis?
Symmetric to origin?



Symmetric to x-axis?

Symmetric to y-axis?

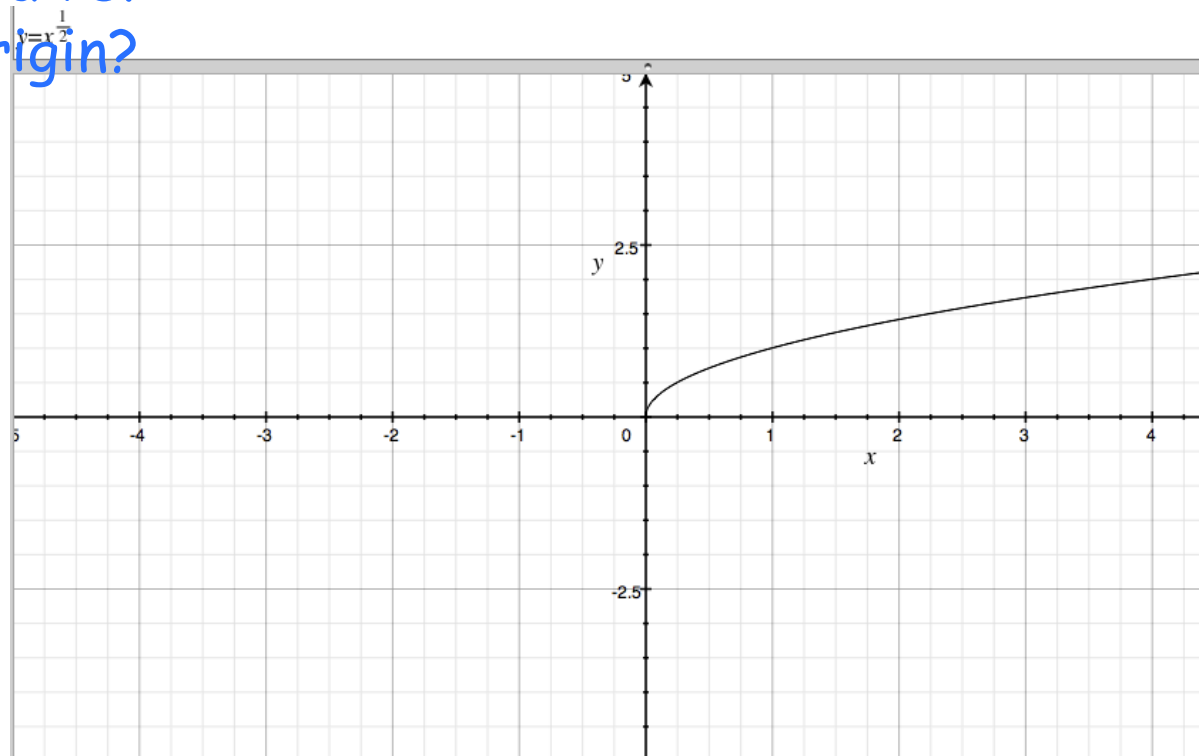
Symmetric to origin?



Symmetric to x-axis?

Symmetric to y-axis?

Symmetric to origin?



Symmetric to x-axis?

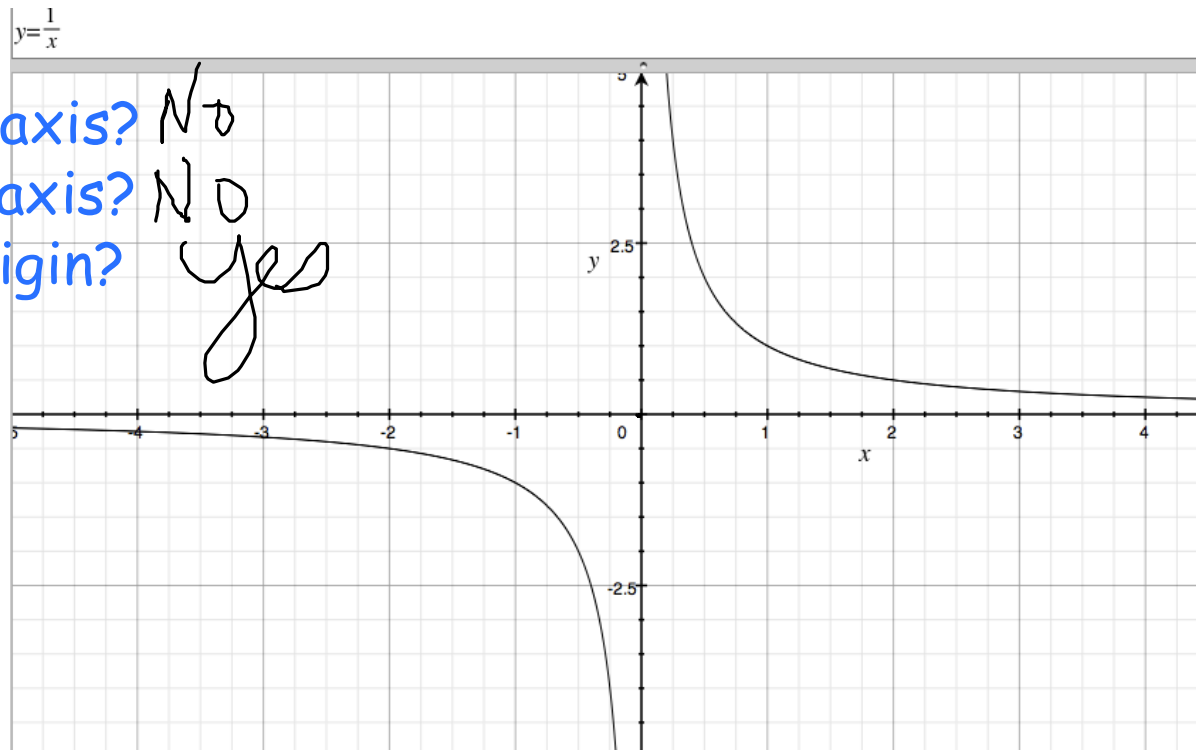
No

Symmetric to y-axis?

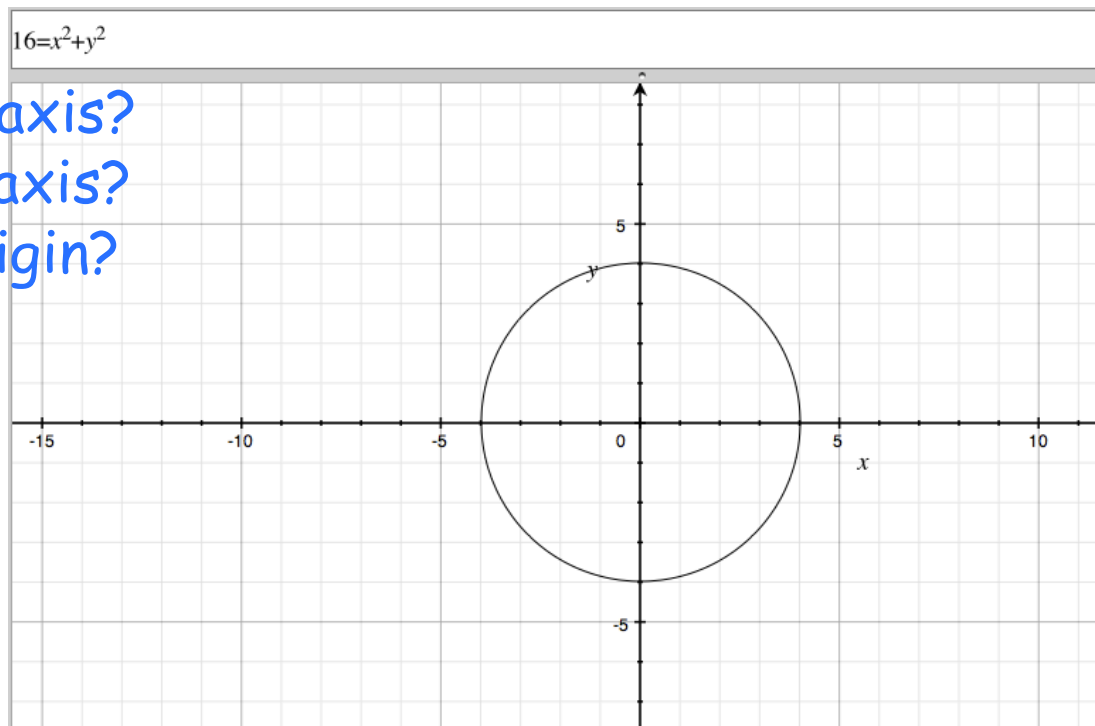
No

Symmetric to origin?

Yes



Symmetric to x-axis?
Symmetric to y-axis?
Symmetric to origin?



$$\frac{x^2}{4} - \frac{y^2}{16} = 1$$

Symmetric to x-axis?

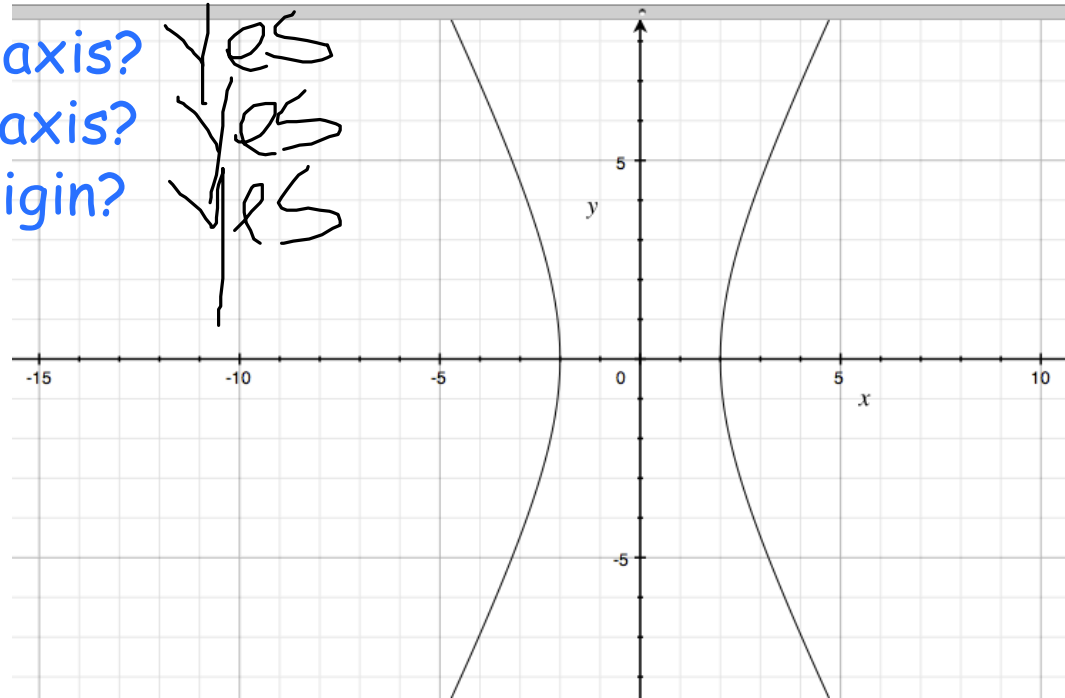
yes

Symmetric to y-axis?

yes

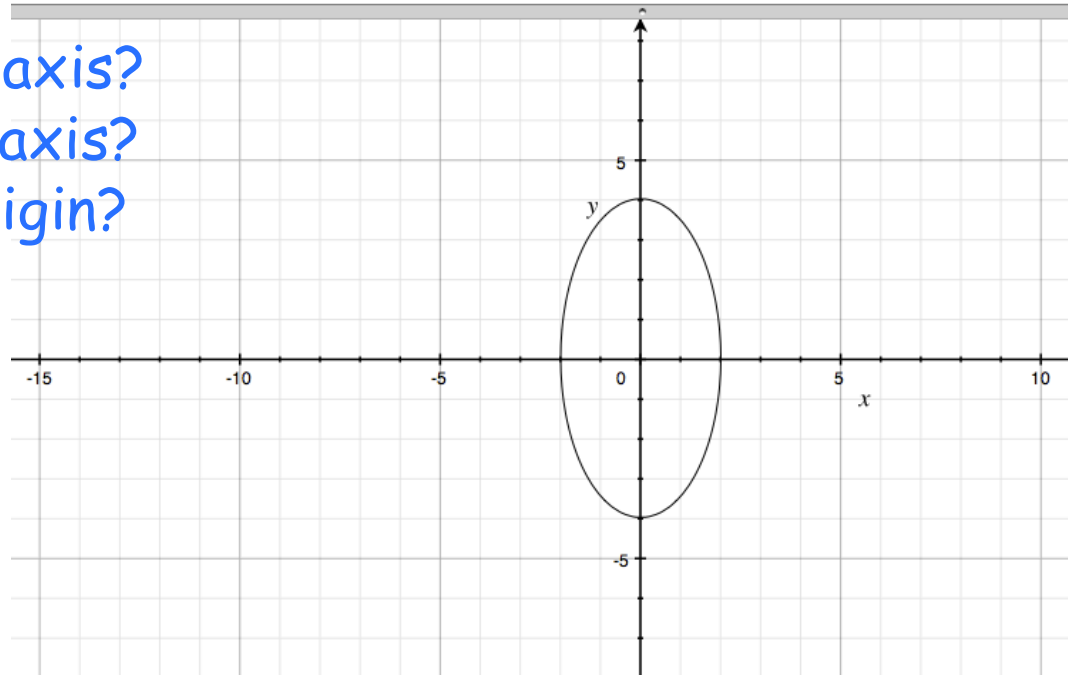
Symmetric to origin?

yes



$$\frac{x^2}{4} + \frac{y^2}{16} = 1$$

Symmetric to x-axis?
Symmetric to y-axis?
Symmetric to origin?



List the x and y intercepts and test for symmetry with the x-axis, y-axis and origin.

x-axis
 $-y \Rightarrow y$
 $(-y)^2 = x$
 $y^2 = x$
Yes

$y^2 = x$

y-axis
 $-x = x$
 $y^2 = -x$
No

Origin
 $-y \Rightarrow y$
 $-x \Rightarrow x$
 $(-y)^2 = -x$
 $y^2 = -x$ No

Example 2

List the x and y intercepts and test for symmetry with the x-axis, y-axis and origin.

$$y^2 - x - 4 = 0$$

Example 3

List the x and y intercepts and test for symmetry with the x-axis, y-axis and origin.

$$y = x^4 - 1$$

Example 4

List the x and y intercepts and test for symmetry with the x-axis, y-axis and origin.

$$y = \frac{x^2 - 4}{2x^4}$$

x-int

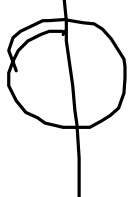
$$0 = \frac{x^2 - 4}{2x^4}$$

$$0 = x^2 - 4$$

$$x = \pm 2$$

$(-2, 0)$ $(2, 0)$

y-int

$$y = \frac{0 - 4}{2(0)}$$


None

x-axis

$$-y \rightarrow y$$

$$-y = \frac{x^2 - 4}{2x^4}$$

$$y = \frac{-x^2 + 4}{2x^4}$$

No

y-axis ~~origin~~

$$-x \rightarrow x$$

$$y = \frac{(-x)^2 - 4}{2(-x)^4}$$

$$y = \frac{x^2 - 4}{2x^4}$$

Yes

Suppose $f(5) = -3$, find another function value given that:

$$\cancel{(-3, 5)} \quad (5, -3)$$

1 - The graph of $y = f(x)$ is symmetric to the x-axis

$$(5, 3) \quad \cancel{(-3, 5)} \quad f(5) = 3 \quad \cancel{f(-3) = 5}$$

2 - The graph of the line $y = f(x)$ is symmetric with respect to the line $y = -2$.

3 - f is an odd function.

Test for symmetry to the x-axis, y-axis and origin.

$$y = 3x^2 + 2$$

$$y = \frac{-3}{x-5}$$

Test for symmetry to the x-axis, y-axis and origin.

$$x = 2y^2 + 5$$

$$xy^3 = -2$$

Test for symmetry to the x-axis, y-axis and origin.

$$x^2 - y^2 = 4$$

$$y = \sqrt[3]{x^2 - 6}$$

Ex7:

Given $f(2)=-6$, find another point of the function if:

a) $f(x)$ is an odd function

b) $f(x)=f(-x)$

c) $f(x)$ is reflected around the x -axis

d) the graph is symmetric to the line of $x=5$

HOMEWORK

p. 246-7: 4-10, 13-20, 31-40

Worksheet: Translations, Reflections, Scalings